

Gravitational-Wave Astronomy

1060-711: Astronomical Observational
Techniques and Instrumentation

Guest Lecturer: Prof. John T. Whelan

2012 May 10

References

- Creighton & Anderson, *Gravitational-Wave Physics and Astronomy* (Wiley, 2011). ISBN 978-3-527-40886-3
- Maggiore, *Gravitational Waves: Volume 1: Theory and Experiments* (Oxford, 2007). ISBN 978-0-198-57074-5
- Saulson, *Fundamentals of Interferometric Gravitational Wave Detectors* (World Scientific, 1994). ISBN 978-9-810-21820-1

Outline

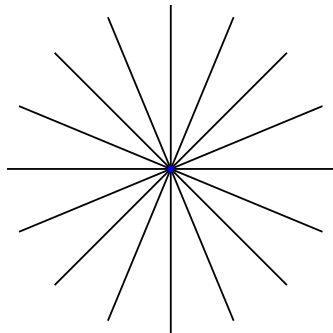
- 1 Gravitational-Wave Physics
 - Physical Motivation
 - Mathematical Description
 - Generation of Gravitational Waves
- 2 Gravitational-Wave Detectors
 - Overview
 - Details of Ground-Based Interferometers
 - Prospects for Space-Based Interferometers
- 3 Gravitational-Wave Astronomy
 - Gravitational Wave Sources
 - Gravitational Wave Data Analysis
 - Selected Results from First-Generation GW Detectors

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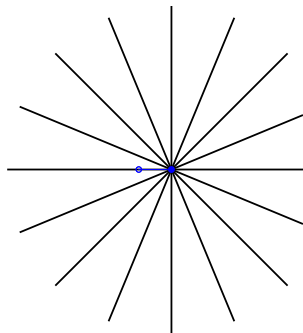
Action at a Distance

- Newtonian gravity:
mass generates
gravitational field
- Lines of force point
towards object



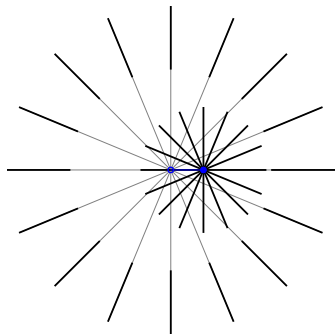
Issues with Causality

- Move object; Newton says:
lines point to new location
- Relativity says:
can't communicate
faster than light
to avoid paradoxes
- You could send me
supraluminal messages
via grav field



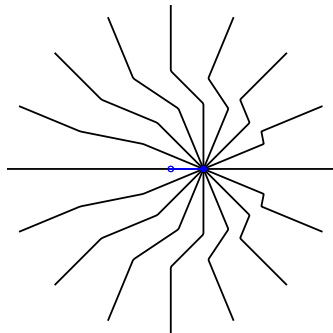
Gravitational Speed Limit

- If I'm 10 light years away, I can't know you moved the object 6 years ago
- Far away, gravitational field lines have to point to old location of the object



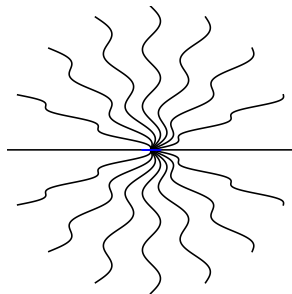
Gravitational Shock Wave

- Sudden motion (acceleration) of object generates gravitational shock wave expanding at speed of light



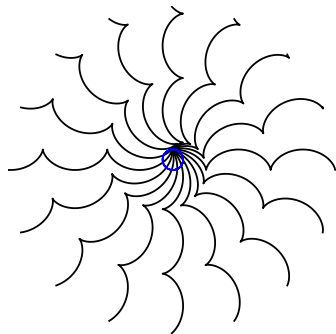
Ripples in the Gravitational Field

- Move object back & forth
→ gravitational wave
- Same argument applies to electricity:
 - can derive magnetism as relativistic effect
 - accelerating charges generate electromagnetic waves propagating @ speed of light

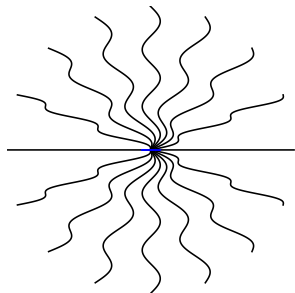
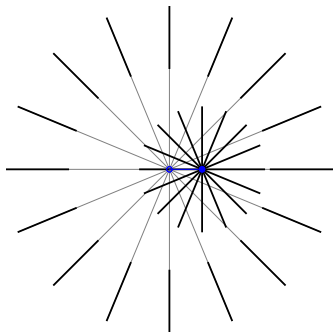


Gravitational Wave from Orbiting Mass?

- Move around in a circle
- Still get grav wave pattern, but looks a bit funny
- Time to move beyond simple pseudo-Newtonian picture



Gravity + Causality = Gravitational Waves



- In **Newtonian gravity**, force dep on distance btwn objects
- If massive object suddenly moved, grav field **at a distance** would change **instantaneously**
- In relativity, **no** signal can travel faster than light
→ time-dep grav fields must propagate like light waves

Gravity as Geometry

- Minkowski Spacetime:

$$ds^2 = -c^2(dt)^2 + (dx)^2 + (dy)^2 + (dz)^2$$
$$= \begin{pmatrix} dt \\ dx \\ dy \\ dz \end{pmatrix}^{\text{tr}} \begin{pmatrix} -c^2 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} dt \\ dx \\ dy \\ dz \end{pmatrix} = \eta_{\mu\nu} dx^\mu dx^\nu$$

- General Spacetime:

$$ds^2 = \begin{pmatrix} dx^0 \\ dx^1 \\ dx^2 \\ dx^3 \end{pmatrix}^{\text{tr}} \begin{pmatrix} g_{00} & g_{01} & g_{02} & g_{03} \\ g_{10} & g_{11} & g_{12} & g_{13} \\ g_{20} & g_{21} & g_{22} & g_{23} \\ g_{30} & g_{31} & g_{32} & g_{33} \end{pmatrix} \begin{pmatrix} dx^0 \\ dx^1 \\ dx^2 \\ dx^3 \end{pmatrix} = g_{\mu\nu} dx^\mu dx^\nu$$

Gravitational Wave as Metric Perturbation

- For GW propagation & detection, work to 1st order in $h_{\mu\nu} \equiv$ difference btwn actual metric $g_{\mu\nu}$ & flat metric $\eta_{\mu\nu}$:

$$g_{\mu\nu} = \eta_{\mu\nu} + h_{\mu\nu}$$

($h_{\mu\nu}$ “small” in weak-field regime, e.g. for GW detection)

- Convenient choice of gauge is **transverse-traceless**:

$$h_{0\mu} = h_{\mu 0} = 0 \quad \eta^{\nu\lambda} \frac{\partial h_{\mu\nu}}{\partial x^\lambda} = 0 \quad \eta^{\mu\nu} h_{\mu\nu} = \delta^{ij} h_{ij} = 0$$

In this gauge:

- Test particles w/constant coörds are **freely falling**
- Vacuum Einstein eqns \implies wave equation for $\{h_{ij}\}$:

$$\left(-\frac{1}{c^2} \frac{\partial^2}{\partial t^2} + \nabla^2 \right) h_{ij} = 0$$

Gravitational Wave Polarization States

- Far from source, GW looks like plane wave prop along \vec{k}
TT conditions mean, in convenient basis,

$$\{k_i\} \equiv \mathbf{k} = \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} \quad \{h_{ij}\} \equiv \mathbf{h} = \begin{pmatrix} h_+ & h_\times & 0 \\ h_\times & -h_+ & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

where $h_+ \left(t - \frac{x^3}{c}\right)$ and $h_\times \left(t - \frac{x^3}{c}\right)$ are components in “plus” and “cross” polarization states

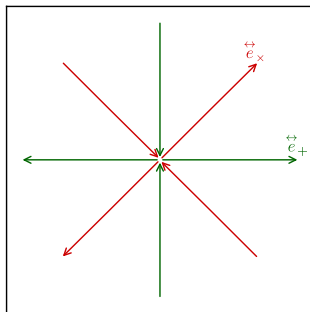
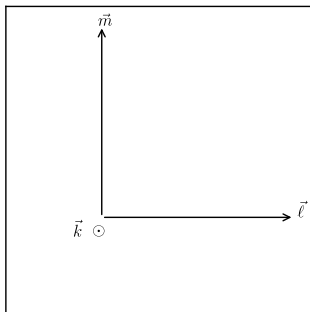
- More generally

$$\overset{\leftrightarrow}{h} = h_+ \left(t - \frac{\vec{k} \cdot \vec{r}}{c}\right) \overset{\leftrightarrow}{e}_+ + h_\times \left(t - \frac{\vec{k} \cdot \vec{r}}{c}\right) \overset{\leftrightarrow}{e}_\times$$

The Polarization Basis

- wave propagating along \vec{k} ;
construct $\vec{e}_{+,x}$ from \perp unit vectors \vec{l} & \vec{m} :

$$\vec{e}_+ = \vec{l} \otimes \vec{l} - \vec{m} \otimes \vec{m} \quad \vec{e}_x = \vec{l} \otimes \vec{m} + \vec{m} \otimes \vec{l}$$



Effects of Gravitational Wave

Fluctuating geom changes distances btwn particles in free-fall:

| Plus (+) Polarization | Cross (\times) Polarization |
|-----------------------|---------------------------------|
| | |

Multipole Expansion for Gravitational Radiation

- **“Electric Dipole”?**
No, “dipole moment” $\int \vec{r} dm \propto$ ctr of mass
COM can't oscillate (also no **negative “charge”** in GR)
- **“Magnetic Dipole”?** No, “mag moment”
 $\frac{1}{2} \int \vec{r} \times \vec{v} dm \propto$ spin, another conserved quantity
- **“Electric Quadrupole”?** Yes! In TT gauge,

$$h_{ij}(t) = \frac{2G}{c^4 d} P^{\text{TT}k\ell}_{ij} \ddot{t}_{k\ell}(t - d/c)$$

in terms of mass quadrupole moment

$$t_{ij} = \int \left(r_i r_j - \delta_{ij} \frac{r^2}{3} \right) dm$$

Quadrupole Radiation From Rotating/Orbiting System

- Equatorial moments of inertia I_1, I_2

- Orbital/rotational ang vel Ω

- GW frequency

$$f_{\text{gw}} = 2 \frac{\Omega}{2\pi}$$

- Since $\ddot{I} \sim (2\Omega)^2 |I_1 - I_2|$,

$$\overset{\leftrightarrow}{h} = \frac{4G\Omega^2(I_1 - I_2)}{c^4 d} \left(\overset{\leftrightarrow}{e}_+ \frac{1 + \cos^2 \iota}{2} \cos 2\Omega t + \overset{\leftrightarrow}{e}_\times \cos \iota \sin 2\Omega t \right)$$

- For binary system w/masses m_1, m_2 and separation r ,

$$I_1 = 0 \quad \text{and} \quad I_2 = \mu r^2$$

where $\mu = \frac{m_1 m_2}{m_1 + m_2} = \frac{m_1 m_2}{M}$ is the reduced mass

Radiation from Quasicircular Binary

Total mass $M = m_1 + m_2$; reduced mass $\mu = \frac{m_1 m_2}{M}$; orbital freq Ω

- Amplitude is $h_0 = \frac{4G\Omega^2 \mu r^2}{c^4 d}$
- Kepler's 3rd law: $GM = r^3 \Omega^2 \implies r^2 = (GM\Omega^{-2})^{2/3}$
 $h_0 = \frac{4G^{5/3} M^{2/3} \mu \Omega^{2/3}}{c^4 d} = \frac{4(GM_c)^{5/3} \Omega^{2/3}}{c^4 d}$
where $M_c = M\eta^{3/5}$ is **chirp mass** & $\eta = \frac{\mu}{M}$ is **symm mass ratio**
- Orbit will evolve due to GW emission (radiation reaction):
energy lost, r dec., Ω inc., h_0 inc.: "chirp"
- Quasicircular assumption breaks down when
 $r_{\text{isco}} \approx 6GM/c^2$ near "innermost stable circular orbit"
(ISCO); orbital freq @ ISCO is $\Omega_{\text{isco}} \approx \sqrt{\frac{GM}{r_{\text{isco}}^3}} = \frac{c^3}{6^{3/2} GM}$
- Modelling final merger accurately requires
numerical simulations like those done in RIT CCRG

Some Sources of Gravitational Waves

Band: ground, space, pulsar timing

- Binary coalescence (inspiral+merger+ringdown):
 - Supermassive BH binary
 - extreme mass ratio (stellar mass + SMBH)
 - Stellar mass BH and/or neutron star
- Galactic white dwarf binary orbit (continuous source)
- Rotating neutron star (pulsar, LMXB, etc)
- Supernova, SGR
- Cosmological background
(primordial, phase transitions, cosmic superstrings, etc)
- SMBH flyby

Outline

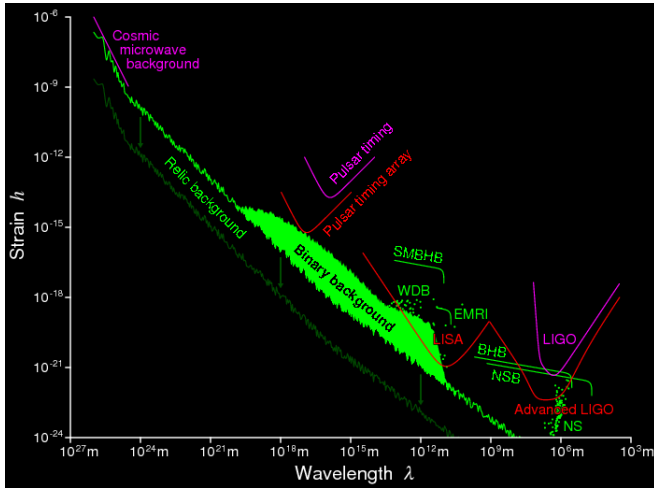
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Methods for Measuring Gravitational Waves

- Cosmic Microwave Background Perturbations ($f_{\text{gw}} \sim H_0 \sim 10^{-18}$ Hz)
- Pulsar Timing Arrays (10^{-9} Hz $\lesssim f_{\text{gw}} \lesssim 10^{-7}$ Hz)
- Laser Interferometers
 - Space-Based (10^{-3} Hz $\lesssim f_{\text{gw}} \lesssim 10^{-1}$ Hz)
 - Ground-Based (10^1 Hz $\lesssim f_{\text{gw}} \lesssim 10^3$ Hz)
- Resonant-Mass Detectors (narrowband, $f_{\text{gw}} \sim 10^3$ Hz)

Note, observable GW freq cover **20** orders of magnitude, similar to EM radiation, but the frequencies are much lower (10^3 Hz $\lesssim f_{\text{em}} \lesssim 10^{23}$ Hz)

The Gravitational-Wave Spectrum



<http://www.tapir.caltech.edu/~teviet/Waves/>

Rogues' Gallery of Ground-Based Interferometers



LIGO Hanford (Wash.)



LIGO Livingston (La.)



GEO-600 (Germany)



Virgo (Italy)

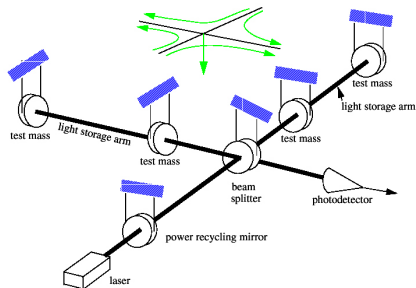
Initial Gravitational Wave Detector Network

- “1st generation” ground-based interferometric GW detectors (kilometer scale):
 - TAMA 300 (Tokyo, Japan) first online, late 90s; now offline
 - LSC detectors conducting science runs since 2002
 - LIGO Hanford (4km H1 & 2km H2)
 - LIGO Livingston (4km L1)
 - GEO-600 (600m G1)
 - Virgo (3km V1) started science runs in 2007
 - LSC-Virgo long joint runs @ design sensitivity 2005-2010
- LIGO and Virgo being upgraded to 2nd generation “advanced” detectors (10× improvement in sensitivity)
- GEO-600 remains operational in “astrowatch” mode in case there’s a nearby supernova

Advanced Gravitational Wave Detector Network

- “2nd generation” ground-based interferometric GW detectors:
 - Adv LIGO expected to take science data from 2014 or 2015
4km detectors in Livingston, La. & Hanford, Wa.
 - Advanced Virgo should be on comparable timescale
 - KAGRA (cryogenic detector in Kamioka mine, Japan)
uses 2.5-generation technology
 - Third advanced LIGO detector (4km)
may be installed in India, taking data c.2019+
Big payoff for sky localization via triangulation
- Planning for 3rd generation already underway:
 - Einstein Telescope in Europe
 - USA 3G plans still under development
(RIT CCRG involved in astrophysics planning)

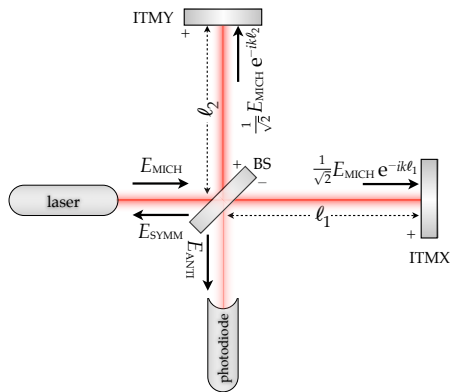
Experimental Details: LIGO



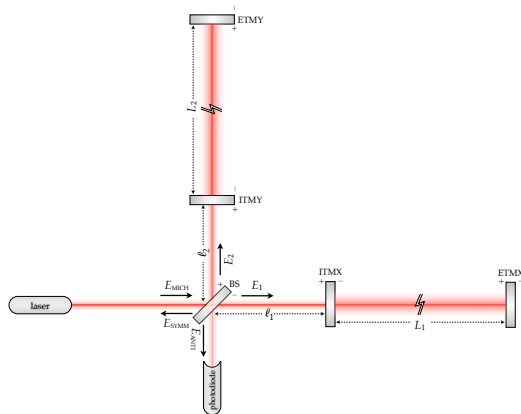
- Initial/enhanced LIGO was a power-recycled Fabry-Pérot Michelson interferometer
- Advanced LIGO will be a dual-recycled Fabry-Pérot Michelson interferometer
- Basic idea: use interferometry to measure changes in difference of arm lengths to detect $h \lesssim 10^{-20}$

Michelson Interferometer

$w/\lambda_{\text{laser}} \sim 10^{-6} \text{ m} \ \& \ L \sim 10^3 \text{ m}$
 would need to measure
 $\delta L \sim 10^{-11} \lambda_{\text{laser}}$
 to detect $h \sim 10^{-20}$

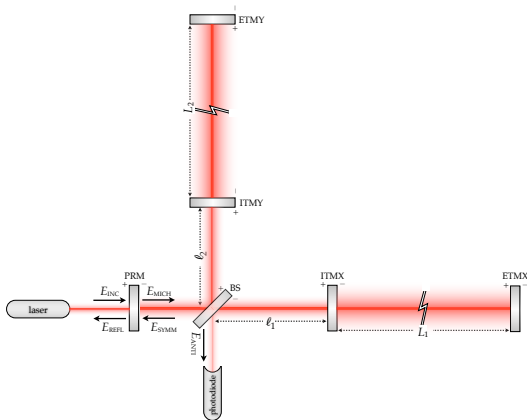


Fabry-Pérot Cavities



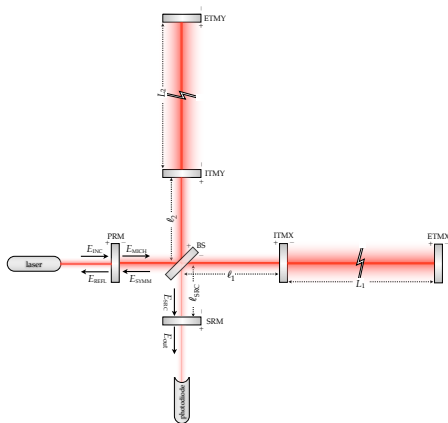
Increase “effective length” of arms by keeping light in resonance within FP cavities; finesse ~ 200 amplifies signal

Power Recycling



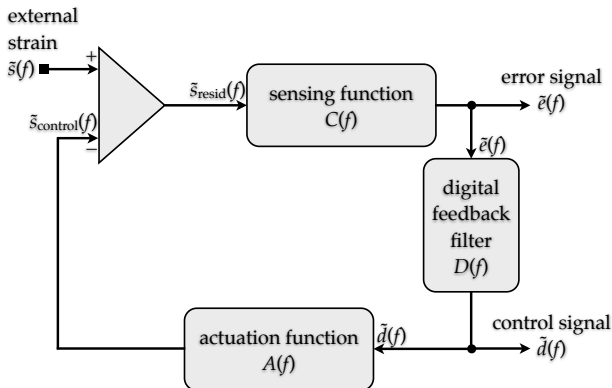
Lengths tuned to keep antisym port dark; power recycling mirror recovers light & sends it back into IFO

Advanced Detectors: Signal Recycling



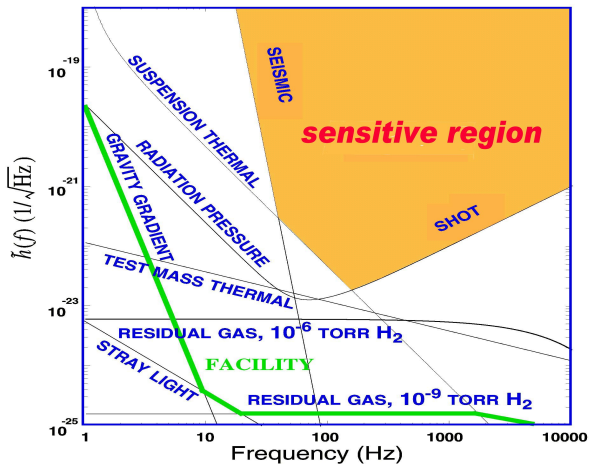
Advanced LIGO/Virgo will also have signal recycling mirror (technology tested by GEO) to decouple noise sources

Sensing, Feedback and Calibration



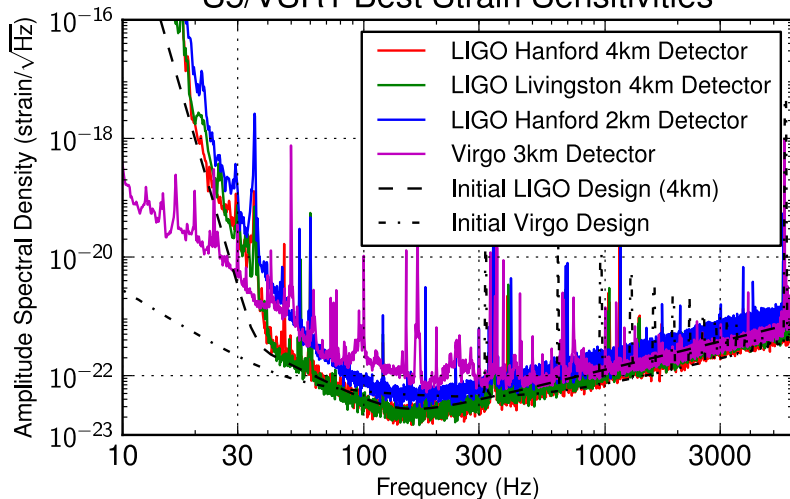
Have to keep FP cavities locked; don't literally let mirrors move in response to GW (& environment); feedback loop keeps IFO in resonance; "GW channel" derived from applied control signal

Sources of Noise in Initial LIGO



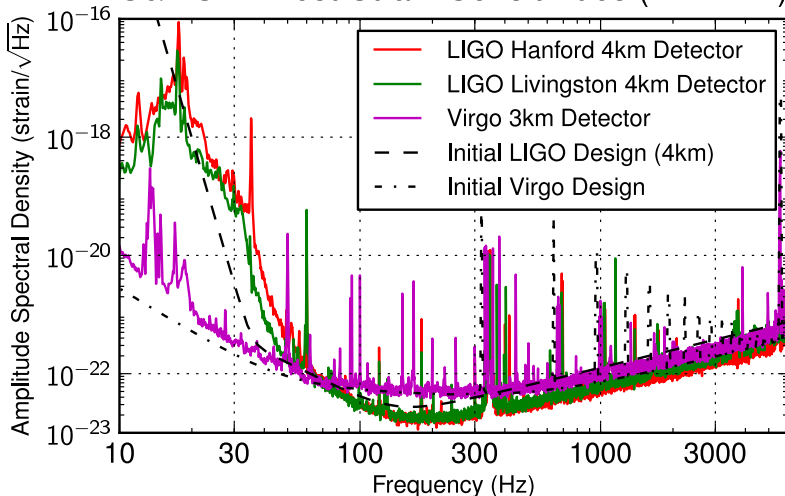
Initial Detector Sensitivities

S5/VSR1 Best Strain Sensitivities

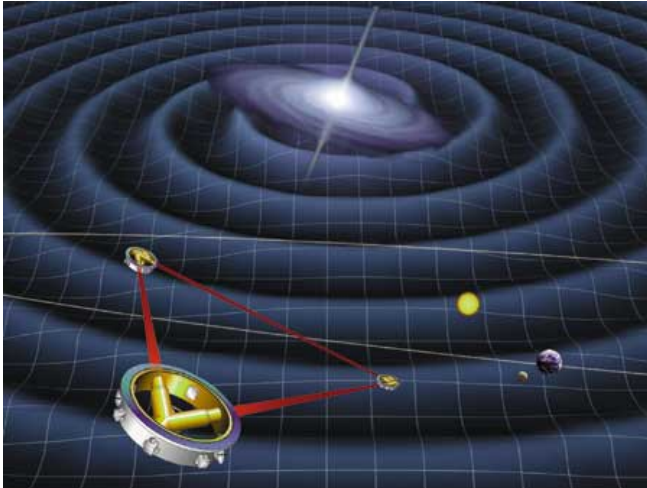


“Enhanced” Detector Sensitivities

S6/VSR2 Best Strain Sensivities (PRELIM)



The Saga of Space-Based GW Detectors



The Saga of Space-Based GW Detectors

- LISA (Laser Interferometer Space Antenna) originally proposed in 1993 for 2011 launch; designed to detect mHz GWs from SMBH, galactic WD binaries, EMRIs, etc
- Planned as joint NASA/ESA mission
- Never got funding wedge; dropped by NASA last year
- ESA considered “NGO” (LISA-lite) for L-class mission; recently opted for JUICE (moons of Jupiter mission)
- LISA/NGO consistently rated high on science by NASA/ESA, but concerns about practicalities
- LISA Pathfinder Mission flies 2014, to demonstrate technology
- Next ESA L-class mission will be selected in 2015; could fly mid-2020s

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Classification of GW Sources

At freqs relevant to ground-based detectors (10s-1000s of Hz),
natural division of sources according to nature of signal

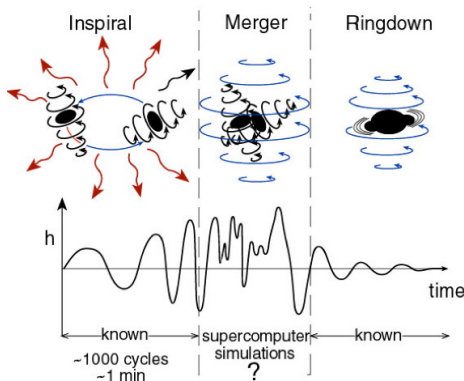
| | modelled | unmodelled |
|-------|---|---|
| long | Periodic Sources (e.g., Rotating Neutron Star) | Stochastic Background (Cosmological or Astrophysical) |
| short | Binary Coalescence (Black Holes, Neutron Stars) | Bursts (Supernova, short BH Merger, etc.) |

Data Analysis Techniques

- **Periodic:** Waveform well-modelled & long-lived
Sky position via **Doppler modulation**
- **Stochastic:** **Cross-correlate** detector outputs
→ Signal-to-noise improves with time
- **Bursts:** Signal unmodelled
→ Look for unusual features & **coherence** btwn detectors
Recent searches incl **GRB triggers**
- **Inspiral:** Signal well modelled (at least early)
→ **Matched Filtering**

Template Waveforms for Binary Coalescence

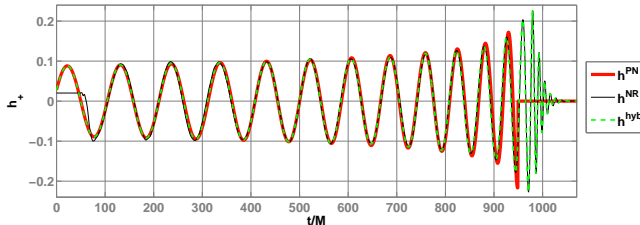
- Inspiralling binaries produce **well-modelled** GW signals;
 Search with **pattern-match filter**
- Compact object binary coalescence consists of
inspiral / **plunge** / **merger** / **ringdown**



Cartoon by Kip Thorne

Template Waveforms for Binary Coalescence

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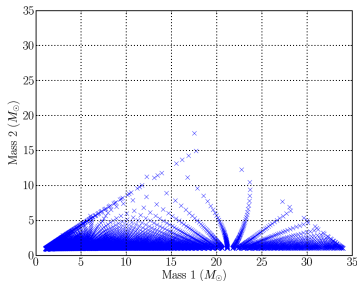
Ajith et al, *CQG* **24**, S689 (2007)

Template Waveforms for Binary Coalescence

- Compact object binary coalescence consists of **inspiral** / **plunge** / **merger** / **ringdown**
- For first part of **inspiral**, orbits **not too relativistic** can expand in powers of $\frac{v}{c}$ → **post-Newtonian** methods
Can estimate **orb vel** from Kepler's 3rd law: $v \approx (\pi GMf)^{1/3}$
 - **Low Mass** → plunge @ **high freq**
 $1.4M_{\odot}/1.4M_{\odot}$ NS/NS binary has $v \approx 0.3c$ @ 800 Hz;
PN OK in LIGO band
 - **High Mass** → plunge @ **low freq**
 $10M_{\odot}/10M_{\odot}$ BH/BH binary has $v \approx 0.4c$ @ 200 Hz;
merges in LIGO band
- Different **template families** used for different **mass ranges**

Matched Filtering GW Data

- Match-filtered **signal-to-noise ratio** measures how well **template** “fits” **data**: $\rho \sim \int df \frac{x^*(f)h(f)}{S_n(f)}$
- Time series for each set of param (e.g., m_1 & m_2) values
- Lay out parameter choices in **template bank** to get good **overlap** w/possible signals



Continuous Waves: Searching for Known Pulsars

- **Phase params** (rotation, sky pos [& binary params]) known Pulsar ephemerides (timing) detail phase evolution
- Can search over **amplitude params** (h_0, ι, ψ, ϕ_0); search cost **NOT** driven by observing time
- Different options for **amplitude parameters**:
 - **Maximize** likelihood analytically (\mathcal{F} -statistic)
 - **Marginalize** likelihood numerically (\mathcal{B} -statistic)
 - Get **posterior prob distribution** w/Markov-Chain Monte Carlo
 - Use astro observations to constrain spin orientation (ι & ψ)
- Spindown produces **indirect upper limit**
 - GW emission above limit \rightarrow more spindown than seen
 - Pulsars w/rapid spindown have “more room” for GW
 - **LIGO/Virgo** have **surpassed spindown** limit for **Crab** & **Vela**

Gravitational Waves from Low-Mass X-Ray Binaries



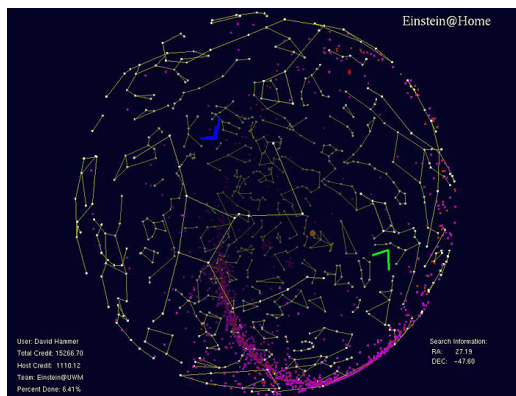
- LMXB: compact object (neutron star or black hole) in binary orbit w/companion star
- If NS, accretion from companion provides “hot spot”; rotating non-axisymmetric NS emits gravitational waves
- Bildsten *ApJL* **501**, L89 (1998) suggested GW spindown may balance accretion spinup; GW strength can be estimated from X-ray flux
- Torque balance would give \approx constant GW freq
- Signal at solar system modulated by binary orbit

Brightest LMXB: Scorpius X-1

- Scorpius X-1
 - $1.4M_{\odot}$ NS w/ $0.4M_{\odot}$ companion
 - **unknown params** are f_0 , $a \sin i$, orbital phase
- LSC/Virgo searches for **Scor X-1**:
 - **Coherent \mathcal{F} -stat search** w/6 hr of S2 data
Abbott et al (LSC) *PRD* **76**, 082001 (2007)
 - Directed stochastic (“**radiometer**”) search (unmodelled)
Abbott et al (LSC) *PRD* **76**, 082003 (2007)
Abbott et al (LSC) *arXiv*:1109.1809
- Proposed directed search methods:
 - Look for **comb of lines** produced by orbital modulation
Messenger & Woan, *CQG* **24**, 469 (2007)
 - **Cross-correlation** specialized to periodic signal
Dhurandhar et al *PRD* **77**, 082001 (2008)
- Promising source for **Advanced Detectors**

Searching for Unknown NSs: Einstein@Home

Semicoherent methods needed to handle phase param space;
Increase computing resources by enlisting volunteers
Distributed using BOINC & run as screensaver



<http://www.einsteinathome.org/>

Searching for a Stochastic Background

- Noisy data from GW Detector:

$$x(t) = n(t) + h(t) = n(t) + \vec{h}(t) : \vec{d}$$

- Look for correlations between detectors

$$\langle x_1 x_2 \rangle = \overbrace{\langle n_1 n_2 \rangle}^{\text{avgto0}} + \overbrace{\langle n_1 h_2 \rangle}^{\text{avgto0}} + \overbrace{\langle h_1 n_2 \rangle}^{\text{avgto0}} + \langle h_1 h_2 \rangle$$

- Expected cross-correlation (frequency domain)

$$\langle \tilde{x}_1^*(f) \tilde{x}_2(f') \rangle = \langle \tilde{h}_1^*(f) \tilde{h}_2(f') \rangle = \vec{d}_1 : \langle \tilde{h}_1^*(f) \otimes \tilde{h}_2(f') \rangle : \vec{d}_2$$

- For stochastic backgrounds

$$\langle \tilde{h}_1^*(f) \tilde{h}_2(f') \rangle = \delta(f - f') \gamma_{12}(f) \frac{S_{\text{gw}}(f)}{2}$$

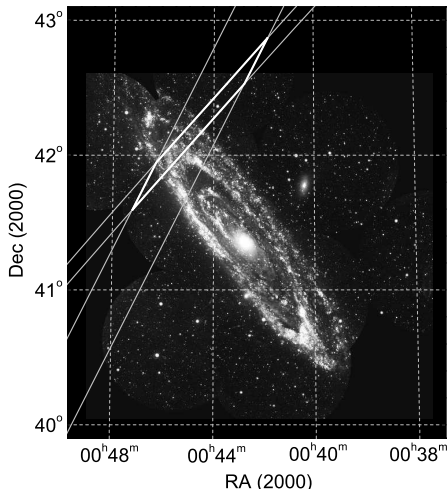
$S_{\text{gw}}(f)$ encodes spectrum; $\gamma_{12}(f)$ encodes geometry

Initial LIGO/Virgo Highlights

- GRB070201 (and GRB051103)
- Crab and Vela spindown
- BBN bound
- Blind Injections

GRB070201

- 2007 Feb 1: short GRB whose **error box** overlapped spiral arm of **M31** (770 kpc away)
- LHO **4 km** & **2 km** detectors operating & sensitive to CBC out to **35.7** & **15.3** Mpc
- No GW seen; **rule out** CBC progenitor in M31 w/ > **99%** conf
- **ApJ 681, 1419 (2008)**



Similar result for GRB051103 & M81; [arXiv:1201.4413](https://arxiv.org/abs/1201.4413)

Crab Pulsar Upper Limit



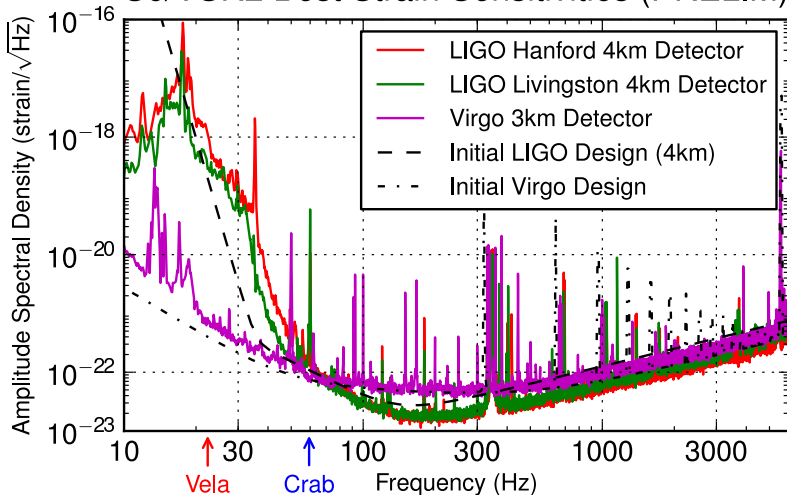
- Pulsar in Crab Nebula
- Created by SN 1054
- ~ 2 kpc away
- $f_{\text{rot}} = 29.7$ Hz
- $f_{\text{gw}} = 59.4$ Hz

Image credit: [Hubble](#)/[Chandra](#)

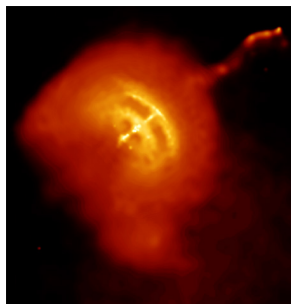
- Initial LIGO (S5) upper limit beats spindown limit
- Abbott et al (LSC) [ApJL 683, L45 \(2008\)](#)
- Abbott et al (LSC & Virgo) + Bégin et al [ApJ 713, 671 \(2010\)](#)
- No more than 2% of spindown energy loss can be in GW

Initial Virgo Targets the Vela Pulsar

S6/VSR2 Best Strain Sensivities (PRELIM)



Vela Pulsar Upper Limit



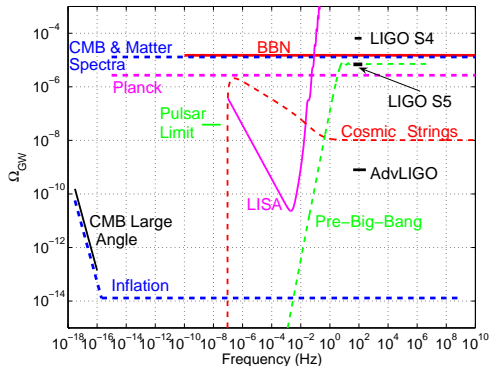
- Pulsar in Vela SN remnant
- Created $\sim 12,000$ years ago
- ~ 300 pc away
- $f_{\text{rot}} = 11.2$ Hz
- $f_{\text{gw}} = 22.4$ Hz

Image credit: **Chandra**

- GW frequency below initial LIGO “seismic wall”
- Virgo has better low-frequency sensitivity
- VSR2 upper limit beats spindown limit
- No more than 10% of spindown energy loss can be in GW

Abadie et al (LSC & Virgo) + Buchner et al *ApJ* **737**, 93 (2011)

Isotropic Stochastic Background Limit



S5 limit $\Omega_{\text{gw}}(f) < 6.9 \times 10^{-6} \left(\frac{72 \text{ km/s/Mpc}}{H_0} \right)^2$
 [Abbott et al (LSC & Virgo) *Nature* **460**, 990 (2009)]
 surpasses indirect limit from Big-Bang Nucleosynthesis

Enhanced LIGO Recovers “Blind Injection”

<http://www.ligo.org/science/GW100916/>

Summary

- Gravitational waves predicted by GR; energetic but couple weakly to matter
- Generated by rapidly changing mass quadrupole moments, e.g., compact object binaries, rotating NSs, supernovae ...
- Current state-of-the-art GW detectors: ground-based interferometers, sensitive at $10^1 - 10^3$ Hz. Initial detectors have set upper limits; advanced detectors should make detections
- Ground-based detectors part of GW spectrum analogous to EM spectrum; multi-wavelength GW observations include space-based detectors (planned, $10^{-3} - 10^{-1}$ Hz) & pulsar timing arrays (operating, $10^{-9} - 10^{-7}$ Hz)